

**II/IV B. TECH DEGREE EXAMINATIONS, JULY/AUGUST-2023****Second Semester****CSE/AM****DISCRETE MATHEMATICS****Time: Three Hours****Maximum: 70 Marks****Answer ONE Question from each unit.****5 x 14 = 70 M****All Questions carry equal marks.****UNIT-I**

1. a) Let R be the relation from the set A on itself and defined by  $R = \{(1,1), (1,3), (3,3), (4,4)\}$  then find the relation matrix.
- b) Discuss converse, contra positive and inverse of an implication with an example.

**(OR)**

2. a) Using of inference, show that  $R \wedge (P \vee Q)$  is a valid conclusion from the premises.  
 $P \vee Q, Q \rightarrow R, P \rightarrow M, \text{ and } \sim M$
- b) Show that  $(\exists x)M(x)$  follows logically from the premises  $(x)(H(x) \rightarrow M(x))$  and  $(\exists x)H(x)$

**UNIT-II**

3. a) Find the number of arrangements of the letters of "TENNESSEE"
- b) In how many ways can a football team of 11 players be selected from 16 players? How many of them will
  - (i) Include 2 particular players?
  - (ii) Exclude 2 particular players?

**(OR)**

4. a) Enumerating r-permutations without repetitions i.e;  $p(n, r) = n(n-1)(n-2)\dots(n-r+1) = \frac{n!}{(n-r)!}$
- b) What is the coefficient of  $x^{12}y^{13}$  in the expansion of  $(x+y)^{25}$ ?

### UNIT-III

5. a) Solve  $a_n - 5a_{n-1} + 6a_{n-2} = 0$  where  $a_0 = 2, a_1 = 3$ .  
 b) Solve  $a_n - 5a_{n-1} + 6a_{n-2} = 2n, n > 2$  with condition the initial  $a_0 = 1, a_1 = 1$  using generating function.

(OR)

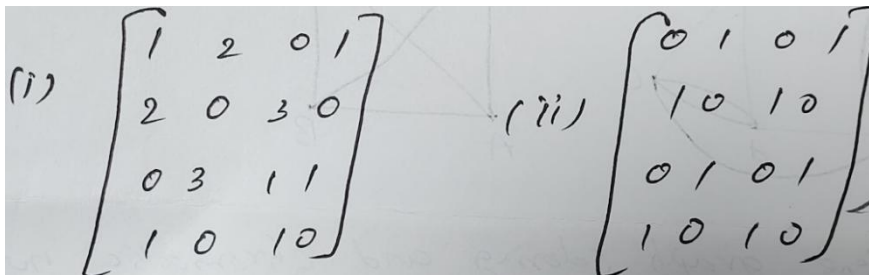
6. a) Let  $A = \{1, 2, 3\}$  and  $R = \{(1, 1), (1, 4), (4, 1), (4, 4), (2, 2), (2, 3), (3, 2), (3, 3)\}$  write the matrix of 'R' and sketch its graph.  
 b) Discuss the various operations on relation.

### UNIT-IV

7. a) Prove that  $(D_8, |)$  is a Lattice where  $D_8$  is the set of all divisors of 8.  
 b) Out of 21 persons, 9 eat vegetables, 10 eat fish and 7 eat eggs. 5 persons eat all three. How many persons eat at least two out of the three dishes?

(OR)

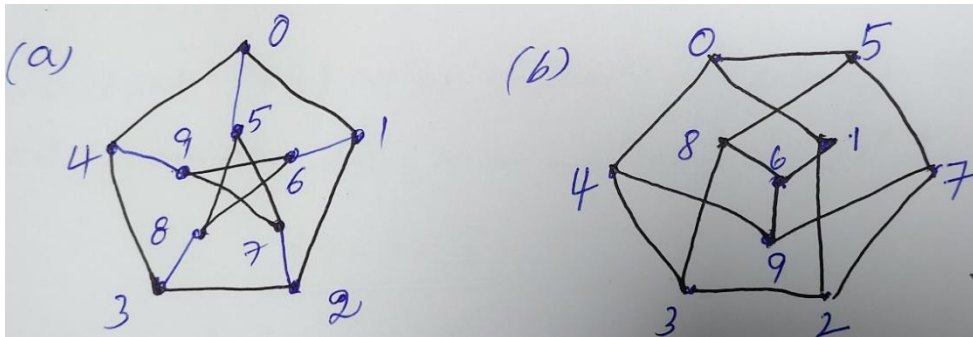
8. a) Draw the graph represented by given adjacency matrix.



- b) If  $A = \{1, 2, 3, 4\}$  and 'R' is a relation on A defined by  $R = \{(1, 2), (1, 3), (2, 4), (3, 2), (3, 3), (3, 4)\}$ , Find  $R_2$  and  $R_3$  and draw its diagram

### UNIT-V

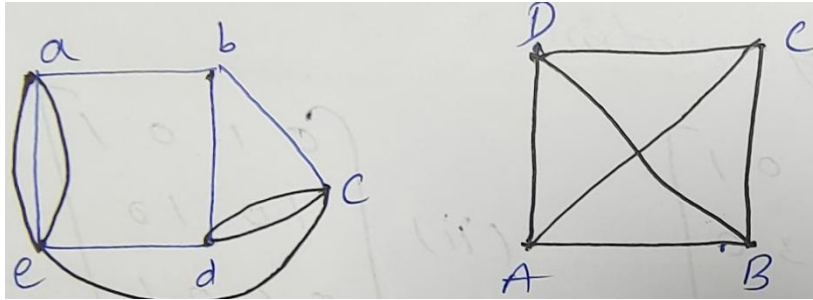
9. a) Examine whether the following graphs are isomorphic or not. Justify your answer.



- b) Explain planar graph, multi graph with examples.

(OR)

10. a) Show that the following graphs are Hamiltonian but not Eulerian.



b) Define graph coloring and chromatic number of a graph and find the chromatic number of  
(i)  $K_{3,3}$                       (ii) cycle with even number of vertices.

